

What is claimed is:

1. A method for determining the value of employee stock options, comprising:

providing a computing module;

inputting into said computer module one or more initial parameters comprising a maturity

5 date, a volatility factor, a dividend yield, an initial stock price, a strike price, a risk-free price, a vesting period, a departure rate, and a blackout date;

outputting from said computing module one or more of an employee optimal exercise

strategy, a probability of departure, a probability of forfeiture, an ESO value, and

one or more calibration metrics including an expected option life, a ratio of a

10 stock price to strike price, an expired worthless probability, and a future stock price.

2. A method of claim 1 further comprising:

computing an employee exercise boundary from said one or more initial parameters;

computing said employee optimal exercise strategy by comparing said future stock price

15 with said employee exercise boundary;

computing an unforced exercised probability from said employee optimal exercise strategy;

computing said probability of forfeiture and a probability of forced exercise from said

probability of departure, said vesting period, said strike price and said future stock

20 price at a date of departure;

computing an ESO value from said probability of forfeiture, said probability of forced exercise and said unforced exercised probability.

3. A method of claim 2 further comprising:

calibrating said one or more initial parameters using a risk aversion factor, an employee wealth parameter and said departure rate.

4. An apparatus for determining the value of employee stock options comprising:

5 a processor configured to:

generate a computing module;

receive as input to said computing module, one or more initial parameters comprising a maturity date, a volatility factor, a dividend yield, an initial stock price, a strike price, a risk-free price, a vesting period, a departure rate, and a blackout date;

10 generate as output from said computing module, one or more of an employee optimal exercise strategy, a probability of departure, a probability of forfeiture, an ESO value, and one or more calibration metrics including an expected option life, a ratio of a stock price to strike price, an expired worthless probability, and a future stock price.

15 5. An apparatus of claim 4 wherein said processor is further configured to:

compute an employee exercise boundary from said one or more initial parameters;

compute said employee optimal exercise strategy by comparing said future stock price with said employee exercise boundary;

compute an unforced exercised probability from said employee optimal exercise strategy;

20 compute said probability of forfeiture and a probability of forced exercise from said probability of departure, said vesting period, said strike price and said future stock price at a date of departure;

compute an ESO value from said probability of forfeiture, said probability of forced exercise and said unforced exercised probability.

6. An apparatus of claim 2 wherein said processor is further configured to:

calibrate said one or more initial parameters using a risk aversion factor, an employee wealth parameter and said departure rate.

7. A method according to claim 1 wherein said computing module determines the following set of values:

a.
$$u = \frac{\gamma + \sqrt{\gamma^2 - 4a^2}}{2a}$$

b.
$$q = \frac{a-d}{u-d}$$

c.
$$V(N, j, k) = U(W_{Nj})$$

d.
$$V(n, j, k) = \begin{cases} V_e, k=0, Bdi(n)=0, V_e > V_c \\ V_e, k=1, Bdi(n)=0, MX > 0 \\ V_c, k=0, Bdi(n)=1 \\ V_c, k=0, Bdi(n)=0, V_e \leq V_c \\ V_f, k=1, Bdi(n)=1 \\ V_f, k=1, Bdi(n)=0, MX \leq 0 \end{cases}$$

e.
$$eev(n, j, k) = \begin{cases} 1, \text{ if } V_e > V_c, Bdi(n)=0, k=0 \\ 1, \text{ if } MX > 0, Bdi(n)=0, k=1 \\ 0, \text{ otherwise} \end{cases}$$

f. $F(n, j, k) = (S_{Nj} - X)^+, \quad j = 0, \dots, N$

g. $CV = e^{-rh} \cdot \left[\left(F(n+1, j+1, 0) \cdot P + F(n+1, j, 0) \cdot (1-P) \right) \cdot P_{stay} + \right. \\ \left. \left(F(n+1, j+1, 1) \cdot P + F(n+1, j, 1) \cdot (1-P) \right) \cdot (1-P_{stay}) \right]$

8. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

5.
$$F(n, j, k) = \begin{cases} eev(n, j, k) \cdot MX + (1 - eev(n, j, k)) \cdot CV, & k = 0 \text{ and } Bdi(n) = 0 \\ CV, & k = 0 \text{ and } Bdi(n) = 1 \\ MX, & k = 1 \text{ and } Bdi(n) = 0 \\ 0, & \text{otherwise} \end{cases}$$

9. A method according to claim 1 wherein said computing module determines the cost of the ESO to an employee using:

a. $U((W_0 + CE)e^{r \cdot h \cdot N}) = V(0, 0, 0)$

10. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

a. $P(0, 0, 0) = 1$

b. $P(n, j, 1) = P(n-1, j, 0) \cdot (1 - P_{stay})$

c. $P(n, 0, 0) = P(n-1, 0, 0) \cdot P_{stay} \cdot (1 - q)$

d. $P(n, n, 0) = P(n-1, n-1, 0) \cdot P_{stay} \cdot q \cdot \delta_{u_n}$

$$e. \quad P(n, j, 0) = P(n-1, j-1, 0) \cdot P_{stay} \cdot q \cdot \text{delta}_u + P(n-1, j, 0) \cdot P_{stay} \cdot (1-q) \cdot \text{delta}_d$$

11. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

$$a. \quad P_{nv} = \sum_{n=0}^{t_v^*} \sum_{j=0}^n P(n, j, 1)$$

- 5 12. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

$$a. \quad \sum_{t_v^*+1}^N \sum_{j=0}^{j^*(n)} P(n, j, 1)$$

13. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

10 a. $\sum_{j=0}^{j^*(n)} P(N, j, 0)$

14. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

$$a. \quad \frac{\sum_{n=t_v^*+1}^N (n \cdot h) \cdot P_t(n)}{\sum_{n'=t_v^*+1}^N P_t(n')}$$

15. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

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$$a. \quad P_e(n) = \sum_{j=0}^n [P(n, j, 0) \cdot eev(n, j, 0) + P(n, j, 1) \cdot \delta_{MX>0}]$$

16. A method according to claim 1 wherein said computing module determines the cost of the ESO using:

$$a. \quad \sum_{i=1}^3 W_i \cdot (\bar{X}_i - \hat{X}_i)^2$$

- 5 17. A method according to claim 1 wherein said computing module determines the cost of the ESO by determining one of more of a stochastic departure rate, constant dividend amount, time varying parameter, or graded vesting.

18. A method according to claim 1 wherein said computing module determines the cost of the ESO by using a strike price that varies according to an index.

- 10 19. A method according to claim 1 wherein said computing module determines the cost of the ESO by using a resettable strike price.

20. A method according to claim 1 wherein said computing module determines the cost of the ESO where an employee pays a fraction of the strike price at a grant date and the remainder of the strike price when the option is exercised.

- 15 21. A method according to claim 1 wherein said computing module determines the cost of the ESO where an option does not vest until a stock price equals or exceeds a given value.

22. A method according to claim 1 wherein said computing module determines the cost of the ESO using a trinomial model.

23. An apparatus of claim 4 wherein said processor is further configured to determine the following set of values:

$$a. \quad u = \frac{\gamma + \sqrt{\gamma^2 - 4a^2}}{2a}$$

$$b. \quad q = \frac{a-d}{u-d}$$

$$5 \quad c. \quad V(N, j, k) = U(W_{Nj})$$

$$d. \quad V(n, j, k) = \begin{cases} V_e, k=0, Bdi(n)=0, V_e > V_c \\ V_e, k=1, Bdi(n)=0, MX > 0 \\ V_c, k=0, Bdi(n)=1 \\ V_c, k=0, Bdi(n)=0, V_e \leq V_c \\ V_f, k=1, Bdi(n)=1 \\ V_f, k=1, Bdi(n)=0, MX \leq 0 \end{cases}$$

$$e. \quad eev(n, j, k) = \begin{cases} 1, \text{ if } V_e > V_c, Bdi(n)=0, k=0 \\ 1, \text{ if } MX > 0, Bdi(n)=0, k=1 \\ 0, \text{ otherwise} \end{cases}$$

$$f. \quad F(n, j, k) = (S_{Nj} - X)^+, \quad j = 0, \dots, N$$

$$g. \quad CV = e^{-rh} \cdot \left[\left(F(n+1, j+1, 0) \cdot P + F(n+1, j, 0) \cdot (1-P) \right) \cdot P_{stay} + \left(F(n+1, j+1, 1) \cdot P + F(n+1, j, 1) \cdot (1-P) \right) \cdot (1-P_{stay}) \right]$$

- 10 24. An apparatus of claim 4 wherein said processor is further configured to determine

$$F(n, j, k) = \begin{cases} \text{eev}(n, j, k) \cdot MX + (1 - \text{eev}(n, j, k)) \cdot CV, & k = 0 \text{ and } Bdi(n) = 0 \\ CV, & k = 0 \text{ and } Bdi(n) = 1 \\ MX, & k = 1 \text{ and } Bdi(n) = 0 \\ 0, & \text{otherwise} \end{cases}$$

25. An apparatus of claim 4 wherein said processor is further configured to determine

a. $U((W_0 + CE)e^{r \cdot h \cdot N}) = V(0, 0, 0)$

26. An apparatus of claim 4 wherein said processor is further configured to determine

5 a. $P(0, 0, 0) = 1$

b. $P(n, j, 1) = P(n-1, j, 0) \cdot (1 - P_{\text{stay}})$

c. $P(n, 0, 0) = P(n-1, 0, 0) \cdot P_{\text{stay}} \cdot (1 - q)$

d. $P(n, n, 0) = P(n-1, n-1, 0) \cdot P_{\text{stay}} \cdot q \cdot \text{delta}_u$

e. $P(n, j, 0) = P(n-1, j-1, 0) \cdot P_{\text{stay}} \cdot q \cdot \text{delta}_u + P(n-1, j, 0) \cdot P_{\text{stay}} \cdot (1 - q) \cdot \text{delta}_d$

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27. An apparatus of claim 4 wherein said processor is further configured to determine

a. $P_{nv} = \sum_{n=0}^{t_v^*} \sum_{j=0}^n P(n, j, 1)$

28. An apparatus of claim 4 wherein said processor is further configured to determine

$$a. \sum_{i_v^*+1}^N \sum_{j=0}^{j^*(n)} P(n, j, 1)$$

29. An apparatus of claim 4 wherein said processor is further configured to determine

$$a. \sum_{j=0}^{j^*(n)} P(N, j, 0)$$

30. An apparatus of claim 4 wherein said processor is further configured to determine

$$5 \quad a. \frac{\sum_{n=i_v^*+1}^N (n \cdot h) \cdot P_i(n)}{\sum_{n'=i_v^*+1}^N P_i(n')}$$

31. An apparatus of claim 4 wherein said processor is further configured to determine

$$a. P_e(n) = \sum_{j=0}^n [P(n, j, 0) \cdot ev(n, j, 0) + P(n, j, 1) \cdot \delta_{MX>0}]$$

32. An apparatus of claim 4 wherein said processor is further configured to determine

$$a. \sum_{i=1}^3 W_i \cdot (\bar{X}_i - \hat{X}_i)^2$$

10 33. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO by determining one of more of a stochastic departure rate, constant dividend amount, time varying parameter, or graded vesting.

34. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO by using a strike price that varies according to an index.

35. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO by using a resettable strike price.

36. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO where an employee pays a fraction of the strike price at a grant date and the remainder of the strike price when the option is exercised.

37. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO where an option does not vest until a stock price equals or exceeds a given value.

38. An apparatus of claim 4 wherein said processor is further configured to determine the cost of the ESO using a trinomial model.